

Directions: Calculators are not allowed. Show any work on a separate sheet of paper and attach. Express any imaginary answers in terms of "i".

Perform the indicated operation. Express your answer as a real or complex number.

- |                          |                          |                          |
|--------------------------|--------------------------|--------------------------|
| 1) $(4 - 6i) + (2 - i)$  | 2) $(8 + 4i) + (6 - 2i)$ | 3) $(7 + 3i) - (2 - 5i)$ |
| 4) $(2 - 6i) - (3 - 2i)$ | 5) $6i(2i)$              | 6) $(4 + i)(4 - i)$      |
| 7) $(2 + 5i)(3 - i)$     | 8) $(6 + 2i)(1 + 5i)$    | 9) $\frac{5}{2+i}$       |
| 10) $\frac{6}{3-2i}$     | 11) $\frac{3+3i}{2+5i}$  | 12) $\frac{4-2i}{1-4i}$  |

If  $i = \sqrt{-1}$ , find the value of each of the following:

- 13)  $i^2$       14)  $i^3$       15)  $i^4$       16)  $i^5$       17)  $i^{10}$       18)  $i^{12}$

Plot each of the following complex numbers on a single grid and label with the given letter.

- 19) A:  $3 + 2i$       20) B:  $-5 + i$       21) C:  $2 - 4i$       22) D:  $-1 - 3i$

Find the solutions to the following equations. Express any imaginary numbers in terms of "i".

- 23)  $x^2 + 4x + 8 = 0$       24)  $3x^2 - 4 = 71$       25)  $x^2 - 2x - 24 = 0$       26)  $x^2 = 8x$
- 27)  $x^2 + 36 = 0$       28)  $2x^2 - x + 5 = 0$       29)  $2x^2 + 3x - 5 = 0$

30) There are two numbers with the following properties.

- 1) The second number is 3 more than the first number.
- 2) The product of the two numbers is 9 more than their sum.

Which of the following represents possible values of these two numbers?

- A) -6, -3      B) -4, -1      C) -1, 4      D) 4, 1

31) What are the zeros of the function  $f(x) = x^2 - x - 12$ ?

32) What are the x-intercepts of the graph of  $y = 3x^2 - 13x - 10$ ?

33) Determine the maximum value of the function  $f(x) = -2(x-3)^2 + 4$ .

34) Determine the minimum value of the function  $f(x) = 5(x+2)^2 + 3$ .

- 35) What is the minimum point of  $y = x^2 + 6x - 4$ ?
- 36) What is the maximum point of  $y = -x^2 - 8x + 5$ ?
- 37) Write the equation  $y = 2x^2 - 20x + 1$  in the completed square form:  $y = a(x-h)^2 + k$
- 38) If  $0 < a < 1$ , how does the graph of  $y = ax^2$  compare to the graph of  $y = x^2$ ?
- 39) If  $a > 1$ , how does the graph of  $y = ax^2$  compare to the graph of  $y = x^2$ ?
- 40) If  $a < 0$ , how does the graph of  $y = ax^2$  compare to the graph of  $y = x^2$ ?
- 41) Describe the translation of the graph  $y = (x+5)^2 + 2$  to the graph of  $y = (x-1)^2 - 3$ .
- 42) Describe the translation of the graph  $y = (x-2)^2 - 1$  to the graph of  $y = (x+6)^2 - 4$ .

Problems 43 - 45: Given the following statements, which ones would be true for the following pairs of parabolas. More than one statement may be true.

- A) Their vertices are maximums.
- B) The graphs have the same shape with different vertices.
- C) The graphs have different shapes with different vertices.
- D) One graph has a vertex that is a maximum, while the other graph has a vertex that is a minimum.
- E) Their vertices are minimums.

43)  $y = -4(x+5)^2 - 3$  and  $y = -4(x+5)^2 + 3$

44)  $y = 2(x+8)^2 + 4$  and  $y = -3(x+2)^2 + 1$

45)  $y = 6(x+2)^2 - 7$  and  $y = 6(x+1)^2 - 3$

46) The function  $f(x) = (x-b)^2 + c$  is a parabola that opens upward with a minimum at the vertex point  $(-1, 6)$ . Use this information to find the constants  $b$  and  $c$ .

49) Sketch a graph of  $y = 2(x+2)^2 - 4$ .

50) Sketch a graph of  $y = -\frac{1}{2}(x-1)^2 + 3$ .